

Industrial Automation
(Automação de Processos Industriais)

Supervised Control
of
Discrete Event Systems

<http://www.isr.ist.utl.pt/~pjcro/courses/api0910/api0910.html>

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Syllabus:

...

Chap. 8 - SEDs and Industrial Automation [2 weeks]

Chap. 9 – Supervised Control of SEDs [1 semana]

*** SCADA**

*** Methodologies for the Synthesis of Supervision
Controllers**

*** Failure detection**

Some jokes available in <http://members.iinet.net.au/~ianw/cartoon.html>

The End.

Some pointers on Supervised Control of DES

- History: The SCADA Web, <http://members.iinet.net.au/~ianw/>
Monitoring and Control of Discrete Event Systems
Stéphane Lafortune,
http://www.ece.northwestern.edu/~ahaddad/ifac96/introductory_workshops.html
- Tutorial: <http://vita.bu.edu/cgc/MIDEDS/>
<http://www.daimi.au.dk/PetriNets/>
- Analysers,
and
Simulators: <http://www.nd.edu/~isis/techreports/isis-2002-003.pdf> (Users Manual)
<http://www.nd.edu/~isis/techreports/spnbox/> (Software)
- Bibliography: * Livros de SCADA <http://www.sss-mag.com/scada.html>
* Moody J. e Antsaklis P., “Supervisory Control of Discrete Event Systems using Petri Nets,” Kluwer Academic Publishers, 1998.
* Cassandras, Christos G., "Discrete Event Systems - Modeling and Performance Analysis," Aksen Associates, 1993.
* Yamalidou K., Moody J., Lemmon M. and Antsaklis P.
Feedback Control of Petri Nets Based on Place Invariants
<http://www.nd.edu/~lemmon/isis-94-002.pdf>

Supervision of DES

Supervisory

Control

And

Data

Acquisition

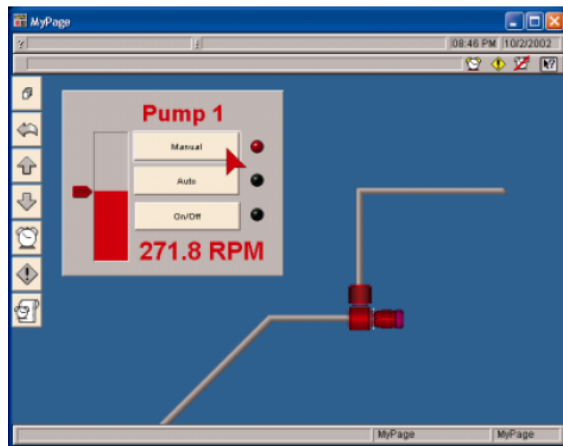
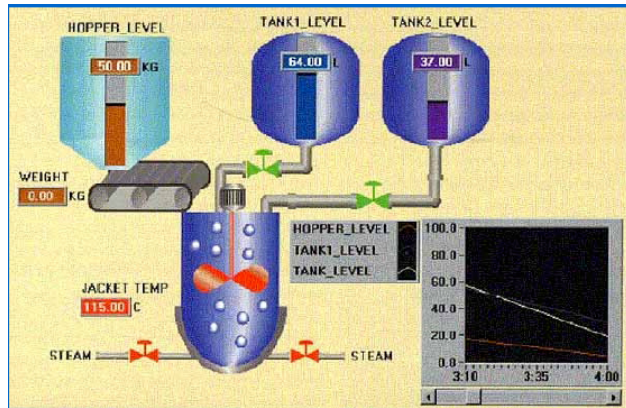
Supervision of DES

SCADA topics

- Remote monitoring of the state of automation systems
- Logging capacity (resorting to specialized Databases)
- Able to access to *historical* information (plots along time, with selectable periodicity)
- Advanced tools to design Human-Machine interfaces
- Failure Detection and Isolation capacity (*threshold* and/or logical functions) on supervised quantities
- Access control

Supervision of DES

Examples of SCADA



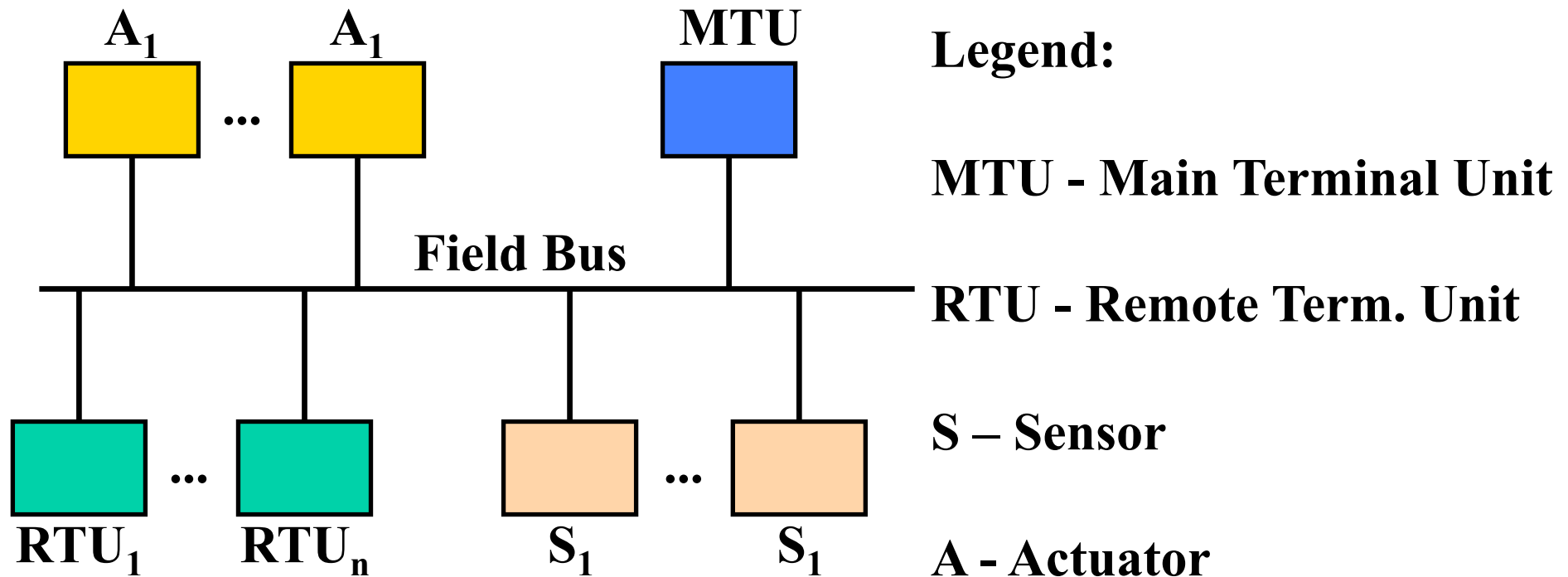
Supervision of DES

Examples of software packages including SCADA solutions

- **Aimax**, de Desin Instruments S.A.
- **CUBE**, Orsi España S.A.
- **FIX**, de Intellution.
- **Lookout**, National Instruments.
- **Monitor Pro**, de Schneider Electric.
- **SCADA InTouch**, de LOGITEK.
- **SYSMAC SCS**, de Omron.
- **Scatt Graph 5000**, de ABB.
- **WinCC**, de Siemens.

Supervision of DES

Hardware Support Architecture of SCADA



Supervision of DES

And

Now

Something

Completely

Different

Supervision of DES

Objectives of the Supervised Control

- Supervise and bound the work of the supervised DES
- Reinforce that some properties are verified
- Assure that some states are not reached
- Performance criteria are verified
- Prevent the deadlock of DES
- Constrain on the use of resources (e.g. mutual exclusion)

Supervision of DES

Some history on Supervised Control

- Methods for finite automata [Ramadge et *al.*], 1989
 - some are based on brute-force search (!)
 - or may require simulation (!)
- Formal verification of *software* in Computer Science (since the 60s) and on *hardware* (90, ...)
- Supervisory Control Method of Petri Nets, method based on *monitors* [Giua et *al.*], 1992.
- Supervisory Control of Petri Nets based on **Place Invariants** [Moody, Antsaklis et *al.*], 1994 (shares some similitude with the previous one, but deduced independently!...).

Supervision of DES

Advantages of the Supervisory Control of Petri Nets

- Mathematical representation is clear (and easy)
- Resorts only to linear algebra (matrices)
- More compact than automata
- Straightforward the representation of infinity state spaces
- Intuitive graphical representation available

The representation of the controller as a Petri Net leads to
simplified Analysis and Synthesis tasks

Supervision of DES

Method of the Place Invariants [ISIS docs]:

What type of relations can be represented in the method of Place Invariants?

- Sets of linear constraints in the state space
- Representation of convex regions (there are extensions for non-convex regions) (?...)
- Constraints to guarantee liveness and to avoid deadlocks (that can be expressed, in general, as linear constraints)
- Constraints on the events and timings (bis)

Supervision of DES

Advantages of the Method of the Place Invariants [ISIS docs]:

Other characteristics that can impact on the solutions?

- Existence and uniqueness
- Optimality of the solutions (e.g. see maximal permissivity next)
- Existence of transition non-controllable and/or not observable (remind definitions for time-driven systems)

In general the solutions can be found solving:

Linear Programming Problems, with Linear Constraints

Methods of Analysis/Synthesis

Method of the Matrix Equations (**just to remind**)

The dynamics of the Petri net state can be written in compact form as:

$$\mu(k+1) = \mu(k) + Dq(k)$$

where:

- $\mu(k+1)$ - marking to be reached
- $\mu(k)$ - initial marking
- $q(k)$ - firing vector (transitions)
- D - incidence matrix. Accounts the balance of tokens, giving the transitions fired.

Methods of Analysis/Synthesis

How to build the Incidence Matrix?

For a Petri net with n places and m transitions

$$\mu \in N_0^n$$

$$q \in N_0^m$$

$$D = D^+ - D^- \in \mathbf{Z}^{n \times m}$$

The enabling firing rule is $\mu \geq D^- q$.

Can also be written in compact form as the inequality

$$\mu + Dq \geq 0,$$

interpreted element by element.

Methods of Synthesis

Some notation for the method

- The supervised system is modelled as a Petri net with n places and m transitions, and incidence matrix

$$D_P \in \mathbb{Z}^{n \times m}.$$

- The supervisor is modelled as a Petri net with n_C places and m transitions, and incidence matrix

$$D_C \in \mathbb{Z}^{n_C \times m}.$$

- The resulting total system has an incidence matrix

$$D \in \mathbb{Z}^{(n+n_C) \times m}.$$

Methods of Synthesis

Theorem: (1) **Synthesis of Controllers based on Place Invariants**

Given the set of linear state constraints that the supervised system must follow, write as

$$L\mu_P \leq b, \quad \mu_P \in N_0^n, \quad L \in Z^{n_C \times n} \quad \text{and} \quad b \in Z^{n_C}.$$

If $b - L\mu_{P_0} \geq 0$, then the controller with incidence matrix and initial marking, respectively

$$D_C = -LD_P, \quad \text{and} \quad \mu_{C_0} = b - L\mu_{P_0},$$

makes the constraints be verified for all markings obtained from the initial marking.

Methods of Synthesis

Theorem:

Proof outline:

The constraint $L\mu_P \leq b$ can be written as

$L\mu_P + \mu_C = b$, using the slack variables μ_C .

They represent the marking of the n_C places of the controller.

To have a place invariant, the relation $x^T D = 0$ must be verified and in particular, given the previous constraint:

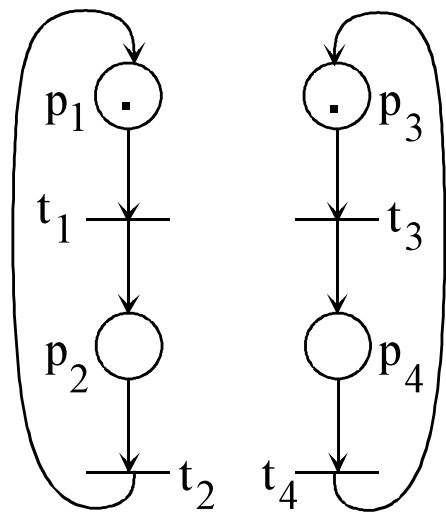
$$x^T D = \begin{bmatrix} L & I \end{bmatrix} \begin{bmatrix} D_P \\ D_C \end{bmatrix} = 0, \text{ resulting } \boxed{D_C = -LD_P.}$$

$$\text{From } L\mu_{P_0} + \mu_{C_0} = b, \text{ follows that } \boxed{\mu_{C_0} = b - L\mu_{P_0}.}$$

Methods of Synthesis

Example of controller synthesis

Mutual Exclusion



Linear constraint: $\mu_2 + \mu_4 \leq 1$

That can be written as:

$$L\mu_P \leq b \quad \begin{bmatrix} 0 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} \mu_1 \\ \mu_2 \\ \mu_3 \\ \mu_4 \end{bmatrix} \leq 1.$$

Incidence Matrix

$$D_P = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

and initial marking

$$\mu_{P_0} = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \end{bmatrix}.$$

Methods of Synthesis

Example of controller synthesis

Mutual Exclusion

1) Test $b - L\mu_{P_0} = 1 - \begin{bmatrix} 0 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \end{bmatrix} = 1 \geq 0.$ **OK.**

2) Compute

$$D_C = -LD_P = -\begin{bmatrix} 0 & 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix} = \begin{bmatrix} -1 & 1 & -1 & 1 \end{bmatrix}$$

and

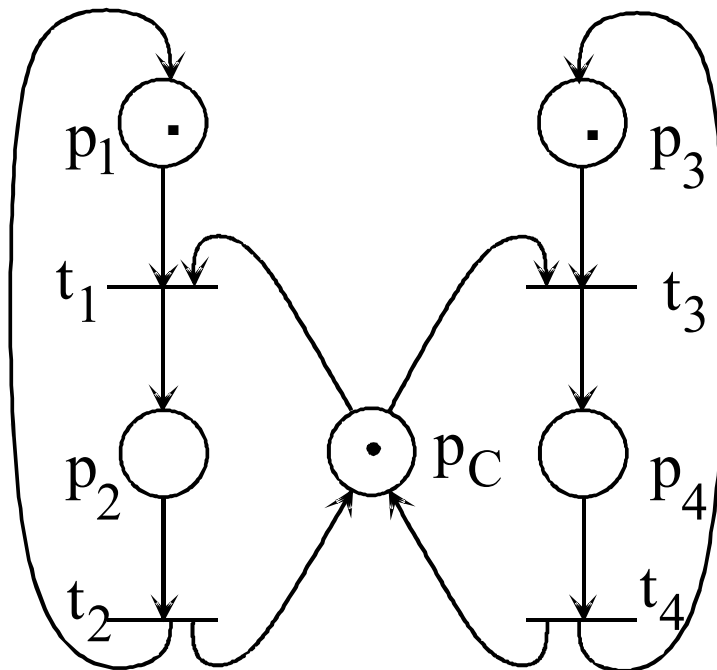
$$\mu_{C_0} = b - L\mu_{P_0} = 1. \quad \text{OK.}$$

Methods of Synthesis

Example of controller synthesis

Mutual Exclusion

3) Resulting in



$$D = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \\ -1 & 1 & -1 & 1 \end{bmatrix}$$

$$\mu_0 = \begin{bmatrix} 1 \\ 0 \\ 1 \\ 0 \\ 1 \end{bmatrix}$$

**OK.
UAU!!!!**

Methods of Synthesis

Definition:

Maximal permissivity occurs when all the linear constraints are verified and all legal markings can be reached.

Lemmas:

- i) The controllers obtained in (1) have maximal permissivity.**

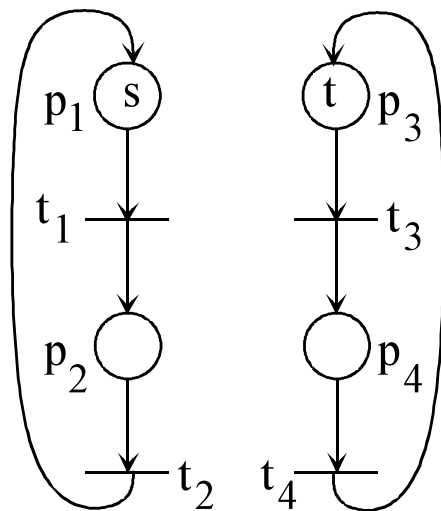
- ii) Given the linear constraints used, the place invariants obtained with the controller synthesized with (1) are the same as the invariants associated with the initial system.**

Methods of Synthesis

Example of controller synthesis

$$\forall s \in N_0, \forall t \in N_0, \forall n \in N_0$$

Readers / Writers



Linear constraints $\mu_2 + n\mu_4 \leq n$
for n books:

That can be written as:

$$L\mu_P \leq b \quad \begin{bmatrix} 0 & 1 & 0 & n \end{bmatrix} \begin{bmatrix} \mu_1 \\ \mu_2 \\ \mu_3 \\ \mu_4 \end{bmatrix} \leq n.$$

Incidence Matrix

$$D_P = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

and initial marking

$$\mu_{P_0} = \begin{bmatrix} s \\ 0 \\ t \\ 0 \end{bmatrix}.$$

Methods of Synthesis

Example of controller synthesis

Readers / Writers

$$1) \text{ Test } \quad b - L\mu_{P_0} = n - \begin{bmatrix} 0 & 1 & 0 & n \end{bmatrix} \begin{bmatrix} s \\ 0 \\ t \\ 0 \end{bmatrix} = n \geq 0. \quad \text{OK.}$$

2) Compute

$$D_C = -LD_P = -\begin{bmatrix} 0 & 1 & 0 & n \end{bmatrix} \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix} = \begin{bmatrix} -1 & 1 & -n & n \end{bmatrix}$$

and

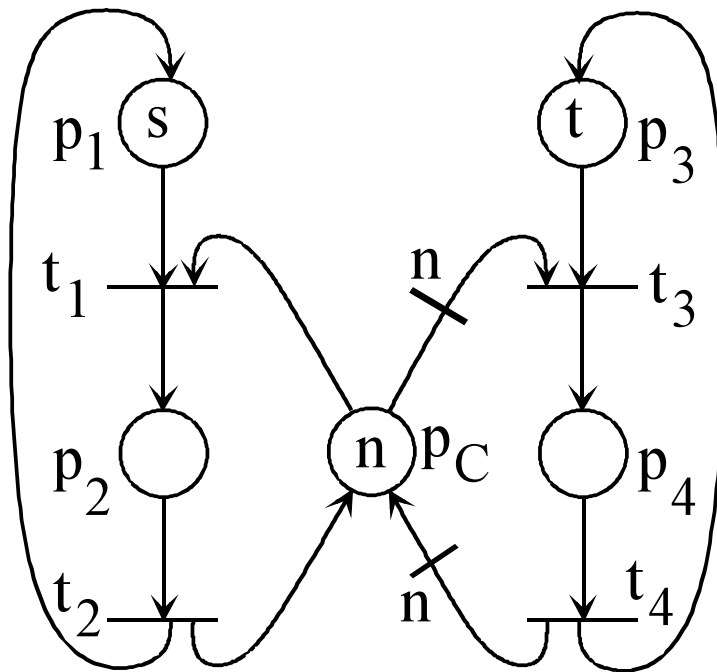
$$\mu_{C_0} = b - L\mu_{P_0} = n. \quad \text{OK.}$$

Methods of Synthesis

Example of controller synthesis

Readers / Writers

3) Resulting in



$$D = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \\ -1 & 1 & -n & n \end{bmatrix}$$

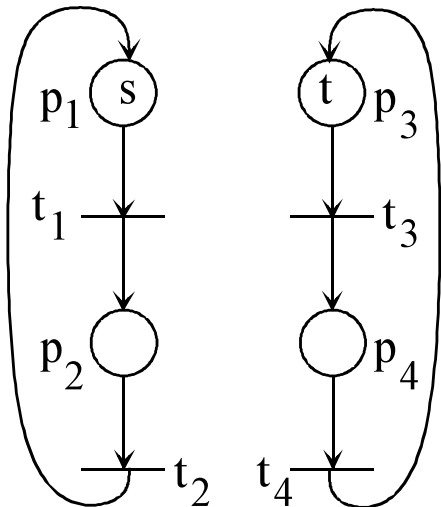
$$\mu_0 = \begin{bmatrix} s \\ 0 \\ t \\ 0 \\ n \end{bmatrix}$$

**OK.
UAU!!!**

Methods of Synthesis

Example of controller synthesis

Producer / Consumer



Incidence matrix

$$D_P = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

Initial marking

$$\mu_{P_0} = \begin{bmatrix} s \\ 0 \\ t \\ 0 \end{bmatrix}$$

What is the linear constraint?

Not possible to write it as a linear constraint $L\mu_P \leq b!$

Is it impossible to solve this problem with the proposed method?

Methods of Synthesis

Generalized linear constraint

Let the generalized linear constraint be

$$\begin{aligned}
 &L\mu_P + Fq_P + Cv_P \leq b, \\
 &\mu_P \in N_0^n, v_P \in N_0^m, q_P \in N_0^m, \\
 &L \in Z^{n_C \times n}, F \in Z^{n_C \times m}, C \in Z^{n_C \times m}, e \quad b \in Z^{n_C},
 \end{aligned}$$

where

- * μ_P is the marking vector for system P;
- * q_P is the firing vector since t_0 ;
- * v_P is the number of transitions (firing) that can occur, also designated as Parikh vector.

Methods of Synthesis

Function LINENF of SPNBOX

Theorem: Synthesis of Controllers based on Place Invariants, for Generalized Linear Constraints

Given the generalized linear constraint $L\mu_P + Fq_P + Cv_P \leq b$,
if $b - L\mu_{P_0} \geq 0$, then the controller with incidence matrix
and initial marking, respectively

$$D_C^- = \max(0, LD_P + C, F)$$

$$D_C^+ = \max(0, F - \max(0, LD_P + C)) - \min(0, LD_P + C),$$

$$\mu_{C_0} = b - L\mu_{P_0} - Cv_{P_0},$$

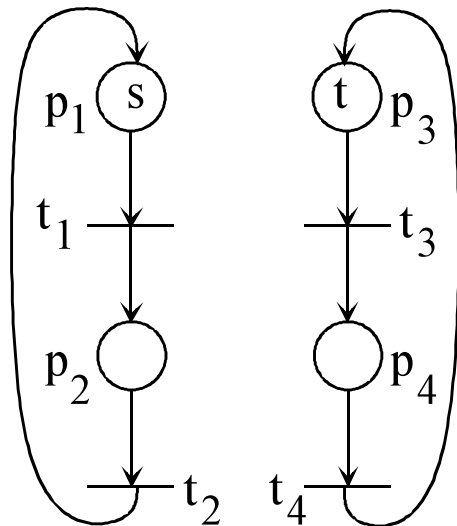
guarantees that constraints are verified for the states resulting
from the initial marking.

Methods of Synthesis

Example of controller synthesis

$$\forall s \in N_0, \forall t \in N_0, \forall n \in N_0$$

Producer / Consumer



Linear constraint: $v_3 \leq v_2$

That can be written as:

$$Cv_P \leq b$$

$$L = 0, F = 0$$

$$\begin{bmatrix} 0 & -1 & 1 & 0 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{bmatrix} \leq 0.$$

Incidence matrix

$$D_P = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

Initial marking

$$\mu_{P_0} = \begin{bmatrix} s \\ 0 \\ t \\ 0 \end{bmatrix}.$$

Methods of Synthesis

Example of controller synthesis

Producer / Consumer

1) Test

$$b - L\mu_{P_0} = 0 - 0 \geq 0.$$

OK.

2) Compute

$$D_C^- = \max(0, [0 \ -1 \ 1 \ 0]0) = [0 \ 0 \ 1 \ 0]$$

$$D_C^+ = \max(0, -[0 \ 0 \ 1 \ 0]) - \min(0, [0 \ -1 \ 1 \ 0]) = \\ = [0 \ 0 \ 0 \ 0] - [0 \ -1 \ 0 \ 0] = [0 \ 1 \ 0 \ 0]$$

e

$$\mu_{C_0} = b - L\mu_{P_0} = 0 - 0 = 0.$$

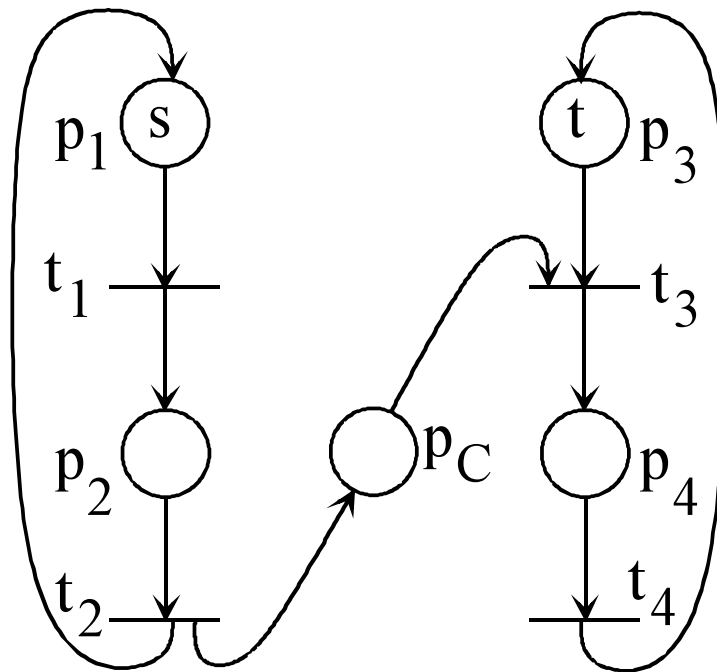
OK.

Methods of Synthesis

Example of controller synthesis

Producer / Consumer

3) Resulting in



$$D = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \\ \mathbf{0 & 1 & -1 & 0} \end{bmatrix}$$

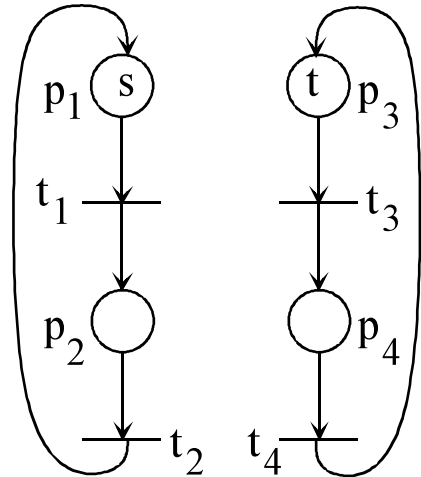
$$\mu_0 = \begin{bmatrix} s \\ 0 \\ t \\ 0 \\ \mathbf{0} \end{bmatrix}$$

**OK.
UAU!!!**

Methods of Synthesis

Example of controller synthesis

Bounded
Producer / Consumer



TWO linear constraints:

$$\forall s \in N_0, \forall t \in N_0, \forall n \in N_0$$

$$v_2 - v_3 \leq n$$

$$v_3 - v_2 \leq n$$

That can be written as:

$$Cv_P \leq b$$

$$L = 0, F = 0$$

$$\begin{bmatrix} 0 & -1 & 1 & 0 \\ 0 & 1 & -1 & 0 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{bmatrix} \leq \begin{bmatrix} n \\ n \end{bmatrix}$$

Incidence matrix

$$D_P = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \end{bmatrix}$$

Initial marking

$$\mu_{P_0} = \begin{bmatrix} s \\ 0 \\ t \\ 0 \end{bmatrix}$$

Methods of Synthesis

Example of controller synthesis

Bounded Producer / Consumer

$$1) \text{ Test } \quad b - L\mu_{P_0} = \begin{bmatrix} n \\ n \end{bmatrix} \geq 0.$$

OK.

2) Compute

$$D_C^- = \max \left(0, \begin{bmatrix} 0 & -1 & 1 & 0 \\ 0 & 1 & -1 & 0 \end{bmatrix}, 0 \right) = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \end{bmatrix},$$

$$D_C^+ = \max \left(0, 0 - \max \left(0, \begin{bmatrix} 0 & -1 & 1 & 0 \\ 0 & 1 & -1 & 0 \end{bmatrix} \right) \right) - \min \left(0, \begin{bmatrix} 0 & -1 & 1 & 0 \\ 0 & 1 & -1 & 0 \end{bmatrix} \right) =$$

$$\begin{bmatrix} 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 \end{bmatrix} - \begin{bmatrix} 0 & -1 & 0 & 0 \\ 0 & 0 & -1 & 0 \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix}.$$

$$\mu_{C_0} = b - L\mu_{P_0} = \begin{bmatrix} n \\ n \end{bmatrix}.$$

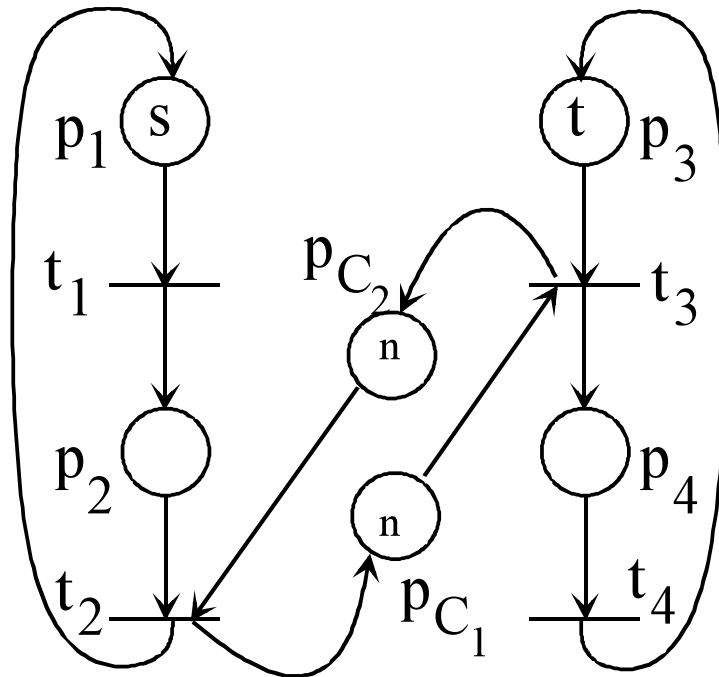
OK.

Methods of Synthesis

Example of controller synthesis

Bounded Producer / Consumer

3) Resulting in



$$D = \begin{bmatrix} -1 & 1 & 0 & 0 \\ 1 & -1 & 0 & 0 \\ 0 & 0 & -1 & 1 \\ 0 & 0 & 1 & -1 \\ 0 & 1 & -1 & 0 \\ 0 & -1 & 1 & 0 \end{bmatrix}$$

$$\mu_0 = \begin{bmatrix} s \\ 0 \\ t \\ 0 \\ n \\ n \end{bmatrix}$$

**OK.
UAU!!!!**

Methods of Synthesis

Definition of Uncontrollable Transition:

A transition is uncontrollable if its firing can be inhibited by an external action (e.g. A supervisory controller).

Definition of Unobservable Transition:

A transition is unobservable if its firing can not be detected or measured (therefore the study of any supervisory controller can not depend from that firing).

Proposition:

A controller can not have arcs that connect to unobservable Transitions, then all unobservable transitions are implicitly uncontrollables.

Methods of Synthesis

Definition: A marking is admissible if

i) $L\mu_P \leq b,$
e

ii)

$$\forall \mu' \in R(C, \mu_{P_0}) \text{ verifies } L\mu' \leq b.$$

Definition: A Linear Constraint is admissible if

i) $L\mu_{P_0} \leq b,$
and

ii) $\forall \mu' \in R(C, \mu_{P_0})$ such that $L\mu' \leq b,$
is an admissible marking.

Methods of Synthesis

Proposition: Admissibility of a constraint

A linear constraint is admissible iff

- The initial markings satisfy the constraint.
- There exist a controller with maximal permissivity that forces the constraint and does not inhibit any uncontrollable transition.

Corolary: given a system with uncontrollable transitions,

$$\boxed{l^T D_{uc} \leq 0} \text{ implies admissibility.}$$

Corolary: given a system with unobservable transitions,

$$\boxed{l^T D_{uo} = 0} \text{ implies admissibility.}$$

Methods of Synthesis

Function MRO_ADM da SPNBOX

Lemma: Structure of Constraint transformation

Let $R_1 \in Z^{n_c \times n}$ such that $R_1 \mu_p \geq 0$,

$R_2 \in Z^{n_c \times n_c}$ be a matrix with positive elements in the diagonal,

If there exists $L' = R_1 + R_2 L$

$$b' = R_2 (b + 1) - 1,$$

such that $L' \mu_p \leq b'$

then it is also verified that $L \mu_p \leq b$.

The End.